FINITE ELEMENT SIMULATION OF THE NORMAL INTERACTION OF PARTICLES IN THE VISCO-ELASTIC SOLID

SUMMARY

This paper addresses the 3D FE simulation of the normal interaction of stiff but deformable particles in binder matrix on the meso-scale. The particles are assumed to be elastic spheres while matrix is considered as viscoelastic solid. The investigation is aimed to capture interaction in terms of normal forces under tension. The problem is considered by applying geometrically linear and nonlinear approaches. Results illustrate influence of initial inter-particle gap reduction of which yields significant increase of the interaction force. Comparison between purely elastic and viscoelastic solutions is also presented.

Keywords: particles, geometric nonlinearity, viscoelasticity, normal interaction force, interface layer

1. INTRODUCTION

Majority of real engineering materials are heterogeneous and multicomponent mixtures, separate components of which possess large diversity of properties on various scales of heterogeneity. Evaluation of mechanical behaviour of them has been the focus of much research over the last decades and various theories and approaches of different complexity are used for characterization purposes.

From the point of view of mechanics the material is regarded as heterogeneous solid. We restrict to particular case of the solid, heterogeneity of which is caused by stiffer particles of different size and properties being the inclusions dispersed in a softer solid matrix. Asphalt-type materials and polymer materials containing coarse aggregates and soft matrix may be regarded as representative prototype of this model. In the case of asphalt, coarse aggregates are stone particles of various shapes and sizes being irregularly distributed in space. The matrix (including binder and fine aggregates) possesses very complex temperature, time and rate dependent behaviour.

Since detailed review is beyond of our purposes, the most characteristic approaches employed for development of deterministic simulation models and selected samples will be mentioned.

In a purely engineering approach, asphalt-type materials are regarded as representative sample. Mechanical behaviour of them is characterized by gradual change of their properties in time under loading. Permanent deformation is one of the considerable load-associated distress types affecting the performance of asphalt mixtures. Comprehensive review on evaluation of mechanical properties is given by [1] and references herein. The mechanistic-empirical approach couples the mechanistic computations with the empirical predictions and the mixture content. The overall accuracy of the mechanistic-empirical models heavily relies upon the quantity and quality of the empirical data used for calibrating of the empirical model. Nevertheless, this approach is widely used in engineering area and various sophisticated models relating macroscopic parameters with composition of particles has been developed.

The use of constrained and unconstrained optimization models in gradation design of hot mix asphalt mixture by Sivilevičius et al. [2] and stochastic optimization by Alavi et al. [1] are referred for the sake of illustration.

Contrary to the engineering empirics, the continuum mechanics based approach provides another alternative. Significant efforts have been made recently, in development of macroscopic models for time-dependent solids. These models are able to capture various viscos and coupled effects in homogenised mixtures or binder components. The Schapery’s single integral model has been widely used to characterize the nonlinear viscoelastic behaviour of engineering materials [3]. Review of viscoelastic models is given in [4]. Example of viscoplastic approach to asphalt concretes is presented in [5]. The viscous models coupled with the non-linear elastic behaviour were considered in [6] and [7].

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The strength of the FEM is existence of complex viscoelastic-viscoplastic constitutive models which can simulate the time-dependent behaviour of continuum. By contrast, the advantages of DE models are that they are conceptually closer to the nature of particulate solids. The main disadvantage may be attributed to description of matrix in a framework of the DE model which is still basically restricted by elastic models.

In spite of extensive research, knowledge about contribution of particular factors to mechanical behaviour of mixtures is not satisfactory. Our investigation addresses the behaviour of the viscoelastic interface between stiffer particles under normal tension loading on the meso-scale. The most attention was focussed towards the role of initial gap to normal tension behaviour. The above problem presents a part of complex issue in development of connecting elements to build efficient but reliable simplified discretisation DE type models.

The paper is organized as follows. The problem is formulated in Section 2, where basic data are also described. The finite element model and its evaluation are given in Section 3. Numerical results and influence of various factors are discussed in Section 4. Final conclusions are drawn in Section 5.

2. PROBLEM DESCRIPTION

2.1. Modelling concept

The approach employed hereafter assumes coarse aggregated mixture as bi-material solid. The particles are assumed to be elastic spheres while the binder matrix is considered as viscoelastic solid. This paper addresses the simulation of the normal interaction under tension on the meso-scale, i.e. on the scale of aggregate, while emphasis is given on evaluation of the size of initial gap between particles.

Evaluation of the interaction may be done in various ways. In our case, the interaction is considered by conducting numerical experiment by applying 3D FEM. Thereby, displacement-driven approach is used to calculate the normal interaction force-displacement relations and stiffness.

2.2. Model description

A pair of elastic spherical particles glued by an interface material is considered hereafter. Actually, the space between and around the particles is fulfilled by viscoelastic binder material. Interaction of two particles is restricted to normal tension. Characterization of the normal interaction is done by considering particles motion in representative volume of the solid. Consequently, this volume is used as the computational domain of numerical model. In our case, geometry of computational domain is presented in a form of circular cylinder containing interacting spheres. Geometry of the central section of computational model is shown in Figure 1.
Geometry of the deformable spheres \( i \) and \( j \) is defined with the radius \( R \). The location of spheres is characterized by the central points \( O_i \) and \( O_j \) referring to local Cartesian coordinates \( \text{Oxyz} \) where axis \( Ox \) points the direction between sphere’s centres. Thus, the centres of spheres are defined by the coordinates \( x_i \) and \( x_j \), respectively.

Location of the cylinder is related to spheres. It is defined by points \( O_i \) and \( O_j \) where cylinder axis coincides local coordinate axis \( Ox \). The initial distance between surfaces of interacting spheres is denoted by \( L_g \).

Geometry of the model cylinder is defined by its length \( L \) and diameter \( H \). It should be clarified that the choice of the cylindrical shape of the interface model is extensively explored in simulations. In the case of bonded granular materials, see Jiang et al. [20], application of the cylinder is quite natural approximation of the bond. Therewith, the cylinder diameter \( H \) is restricted to minimal diameter of interacting particles. It is obvious that deformation behaviour of particles in weaker continuum is slightly different. We can refer to results exhibited by Chareyre et al. [21], where detailed analysis of the viscous flow induced forces acting on the solid particles in dense sphere packing was presented. It was demonstrated that in presence of neighbour particles the representative volume presents composition of tetrahedrons which may approximated by cylindrical volumes.

We focus on mutual interaction of particles. Thus, the length of the imaginary cylinder \( L \) reflects the size of the particle’s radius and the interface gap \( L_g, L = 2R + L_g \). The cylinder diameter \( H \) also depends on the particle’s radius and the thickness of artificially introduced outer cylindrical shell-type layer having thickness \( t_i, H = 2(R + t) \). Presence of this layer gives more freedom to particles motion in the cylinder model and helps to avoid singularities in generation of the FE mesh and numerical simulation.

2.3. Boundary conditions

It is well known that boundary conditions significantly influence the calculation results, especially, during viscous type flows. In our case, boundary conditions are formed to respond behaviour of the representative volume. We restrict ourselves that representative volume is located inside of the global volume, i.e. boundary conditions of the representative volume are not affected by the global boundary condition. Moreover, the influence of neighbour particles, as it used to be in the DE models, is also neglected. The above restrictions imply transversal incompressibility of the cylinder boundary and allow isolated treatment of the particles interaction. Consequently, only the global axial deformation of representative volume is allowed. It is clear, however, that using of incompressible boundary yields the upper bound of the stiffness of the interface layer. Our investigation confirms, that presence of the deformable boundary implemented by the thicker elastic layer up to infinity yields insignificant changes to local deformation and relatively small drop of the inter-particle stiffness.

Because of the axial symmetry the quarter of the half spheres will be considered. Geometry of the computation model with specified boundary conditions is illustrated in Figure 2. Generally, the boundary conditions of the cylinder are assumed to restrict motion of the material into normal outside direction, but can freely slide along the cylinder.

Concerning model sections, the symmetric boundary conditions are specified on the vertical \( O_{ix} \) and horizontal \( O_{iz} \) coordinate planes for both spherical particles and the interface material, i.e. their motion was restricted into normal directions and allows free sliding in tangential direction.

The kinematic boundary conditions were explored to describe the normal loading of the model during numeric simulations. The stretching load is imposed by moving particle \( i \) with respect to fixed particle \( j \) with the displacement value \( u_i \). Actually, the values \( u_i = U \) and \( u_j = 0 \) prescribed to all points of plane sections \( yOix \) and \( xOiy \) including points on the interface material.

The bonded contact between spheres and interface is applied. For consideration of slip or debonding, the finer aggregates should be taken into account, and refined contact layer model is required [10, 22].
2.4. Viscoelasticity relations

Binder material between particles is assumed to be linear viscoelastic. It could be worth to notice that viscoelasticity is the property of materials that exhibit both viscous and elastic characteristics when undergoing deformation. Viscoelastic materials exhibit time-dependent strain behaviour which is result of the diffusion of atoms or molecules inside a material.

It is common approach to present viscoelastic model as linear combinations of elastic and viscous components. In one-dimensional case, the elastic constitutive relationship between the stress $\sigma$ and the strain $\varepsilon$, i.e. Hooke’s law, can be regarded as linear spring with the elasticity constant equal to the elasticity modulus $E$ of the isotropic continuum. The viscous components can be modelled as dashpots such that the linear stress $\sigma$ and the strain rate $\dot{\varepsilon}$ relationship can be characterized by the viscosity coefficient of the material $\eta$ while strain rate $\dot{\varepsilon} = d\varepsilon / dt$ is the time $t$ derivative of strain.

Each of particular viscoelastic models differ in the arrangement of these elements. We employ the Maxwell model (Fig. 3) which defines the strain rate as a sum of elastic and viscous components [3, 6]:

$$\dot{\varepsilon}(t) = \frac{\sigma(t)}{E} + \frac{\sigma(t)}{\eta}$$

(1)

When a material is put under a constant stress $\sigma_0$ the strain is obtained by integration of the rate. Finally, it yields two components

$$\varepsilon(t) = \frac{\sigma_0}{E} + \frac{\sigma_0}{\eta} t$$

(2)

The first, an elastic component occurs instantaneously, corresponding to the spring, and relaxes immediately upon release of the stress. The second is a viscous component that linearly increases with time as long as the stress is applied. In three-dimensions, constitutive relationship is defined in terms of stress and strain tensors, and can be expressed as a hereditary integral [3, 6]:

$$\sigma_{ij}(t) = E_0 \varepsilon_{ij} + \int_0^t E_1 \frac{d\varepsilon_{ij}(\tau)}{d\tau} d\tau$$

(3)

It takes into account that the relaxation does not occur at a single time instant, but varies upon a time. Here, $E_0$ is the constant instantaneous elasticity modulus. The transient part of the material is defined by $E_1$ which is a function of the time $t$ and reflects relaxation of the material stiffness. It is used to describe them with Prony series [15] as follows:

$$E(t) = E_0 \left[ 1 - \sum_{m=1}^{M} \sigma^E_{m \varepsilon} \frac{t}{t_m} \right]$$

(4)

Here, $\sigma^E_{m \varepsilon}$ and $t_m$ are model parameters related to the $m$th component of the Prony series, while $M$ is the number of Prony components in the model. Thereby, $t_m$ is indicator of relaxation speed of the $m$th Prony component.

The stress tensor can be decomposed into the usual sum of volumetric and deviatory parts, $\sigma_{kk}$ and $\sigma_{ij}$, while strain tensor as $\varepsilon_{kk}$ and $\varepsilon_{ij}$, respectively. As a result, constitutive relationship can be decoupled, while each of the components is presented independently in the same manner as (3). Finally, volumetric and deviatory behaviours are described as follows:

$$\sigma_{kk}(t) = 3K_0 \varepsilon_{kk} + 3 \int_0^t K_1 \frac{d\varepsilon_{kk}(\tau)}{d\tau} d\tau$$

(5)

$$\sigma_{ij}(t) = 2G_0 \varepsilon_{ij} + 2 \int_0^t G_1 \frac{d\varepsilon_{ij}(\tau)}{d\tau} d\tau$$

(6)

Here, material properties are defined by is volumetric modulus $K$ and is shear modulus $G$, respectively. By assuming constant Poisson’s ratio $i$ purely elastic case is characterized by instantaneous parameters $K_0$ and $G_0$ expressed via elasticity moduli

$$K_0 = \frac{E_0}{3(1 - 2v)}$$

(7)

$$G_0 = \frac{E_0}{2(1 + v)}$$

(8)

Time variations of $K(t)$ and $G(t)$ them may be described by Prony series according to (4).

2.5. Problem data

Numerical analysis of heterogeneous aggregates presented is accomplished on the scale of coarse aggregates defined hereafter as meso-scale. Problem data for normal interaction are chosen to imitate the behaviour of asphalt concrete presenting aggregate of stone particles embedded into bitumen binder.
The particles are assumed to be perfect spheres to simplify the calculation. They having radius $R = 7.5$ mm. The thickness of artificial outer layer $t_l$ is taken to be 1 mm. Thus, the diameter of the model cylinder (Fig. 2) is defined to be equal $H = 2(R + t_l) = 17$ mm, while its length $L$ reflecting not only the particle's radius $R$ but also the gap $L_g$ is variable parameter.

Mechanical properties of elastic particles are attributed to the features of granite [23]. The Young’s modulus $E$ is equal to $3 \cdot 10^{10}$ Pa while Poisson’s ratio $\nu = 0.25$.

Viscoelastic properties of the binder material respond to the asphalt bitumen and were taken from [24]. They are sensitive to environment temperature and to loading rate. To simplify problem the values responding conditions of the standard Marshall test [25] and defined at fixed temperature equal to $60^\circ$ C and loading rate is $0.847$ mm/s were considered in all examples below.

The Poisson’s ratio is equal to 0.46 and indicates relatively high incompressibility. Time-dependent properties are constant throughout the volume. They are defined by constants of the Maxwell element. Here, time-independent elasticity constant $E_m = 46$ MPa. The values of constants $\alpha_m$ and $t_m$ are given in the Table 1.

<table>
<thead>
<tr>
<th>Component $m$</th>
<th>Factor $\alpha_m$</th>
<th>Time $t_m$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.902</td>
<td>0.637</td>
</tr>
<tr>
<td>2</td>
<td>0.072</td>
<td>6.175</td>
</tr>
</tbody>
</table>

3. THE FINITE ELEMENT MODEL

Simulation of the normal interaction of elastic spheres via viscoelastic interface was conducted by the Finite Element Method. Generation of the model and transient FE analysis was performed by using the FEM ANSYS 13 Workbench software [26].

3.1. Generation of the model

The model domain comprising a quarter of the cylinder shown in Figure 2 was investigated. Geometry of the FE model is defined parametrically and controlled by the basic parameters such as prescribed radius of the particle $R$ and the variable parameter, i.e. the initial size of the gap between particles $L_g$. The tetrahedron type volume elements SOLID187 with 10 nodes were used for generation of the model.

The particles volume is described by coarsest mesh with the average element size equal to 0.1R. The volume of the interface material is conditionally divided into two regions.

The contact region between spheres is divided by the finest mesh with the average element size equal to 0.01R while the remainder region is 0.05R size. The quality of generated mesh was evaluated according to ANSYS requirements [26] by checking by skewness ratio of element.

Sample of, the total FE model consists of 19678 nodes and 9967 elements (Fig. 4). Model sizes, material properties and kinematic boundary conditions were defined in section 2.

![Fig. 4. Finite element mesh of the model domain](image)

3.2. Characterisation of the model properties

Deformation behaviour of the softer interface is characterised by extremely large values of the local strains. Therewith, evaluation of them is important factor has to be conducted by modelling of mixtures. On the results of comprehensive review [10] it was concluded, however, that accurate analytical of solutions of the highly nonlinear problem are not available.

In opposite, the FE code ANSYS and the employed 3D finite element SOLID187 offer many possibilities in terms of various material models and problem formulations. It could be employed for simulating of physical and geometric nonlinearities. Large deflection approach, applicable to static and transient structural analysis, determines automatically whether the solver should take into account large displacements, large rotations and large strains.

The influence of geometric nonlinearity was studied by tracing incrementally the behaviour of the developed model in time. To evaluate particles interaction the geometrically induced loading history is defined as linear function of time while maximal displacement $U = 0.5$ mm is reached after 0.59 s. The sample having the initial gap $L_g = 0.5$ mm was examined.
Simulation results obtained are illustrated in Figure 5, where variations of the normal tension force $F$ via displacement $U$ incrementally are exhibited. The results of the viscoelastic model denoted by bold lines indicate drop of the material properties in time when compared to purely elastic (thin lines). As concerns nonlinearity, it are obvious that finite deflection approach results of which is denoted by solid lines indicates relatively higher displacement values. More precise evaluation shows that neglecting of geometrical nonlinearity overestimates displacement and stiffness. Our sample shows that at the load level $F = 6.0$ N artificial increase of the inter-particle displacement reaches 5% for elastic case and 9% increase for viscoelastic case.

In summary, for the future calculations the large deflection model is preferable.

4. INVESTIGATION OF THE INFLUENCE OF THE INTER-PARTICLE GAP

4.1. Basic statements

Empirical and theoretical investigations show influence of the inter-particle interface material. Current presentation is aimed to influence of the initial inter-particle gap under tension load. The size of the gap means the smallest distance between two surfaces of interacting spheres. The problem is considered numerically, while the concept of the finite element model, along with basic data is described in previous sections. The more realistic large displacement model is exclusively used in simulations. The loading is imposed by moving the spheres in opposite direction until prescribed displacement $U = 0.5$ mm.

Four cases of the model domain with various gap sizes and four finite element models were generated, respectively. The selected values of the gap size $L_1$ equal to 0.1, 0.5, 1.0 and 1.5 mm corresponding to 0.013$R$, 0.066$R$, 0.133$R$ and 0.2$R$, respectively, were considered in the numerical experiment. For further reduction of gap size properties of bitumen film it has to be taken into account.

4.2. Evaluation of the tension force

The tension behaviour of the interface material was basically examined by considering the normal force. The value of the force is extracted from the results of FE calculation. It is obtained as a reaction force of the sphere due to their pulling motion.

Two limit cases corresponding to the sizes of inter-particle gap $L_{g1} = 0.1$ mm and $L_{g4} = 1.5$ mm, respectively, were selected for illustration of the force calculation methodology while the results of viscoelastic samples are examined in details.

Tension force presents resultant contribution of the normal pressure and the tangential traction (frictional pressure). The nature of the force is basically predicted by considering pressure distribution on the sphere. Two different cases of pressure distributions are illustrated in Figure 6. The negative values mean tension (suck) pressure given in Pascal’s.

The pressure colour analysis indicates that for smaller gap (Fig. 6a) the highest values of pressure $p_1(r)$ varying in the range between $p_{1,\text{max}} = 3.47$ MPa and $1.16$ MPa are concentrated within the small circle having radius $r = 0.1R$. The of distribution pressure $p_4(r)$ in another sample is much different (Fig. 6b). It has a gradual decreasing character while the maximal pressure $p_{4,\text{max}} = 0.2$ MPa is almost 18 times lower. Another observation is that values of the tangential traction are in average about 10 times lower.

Calculation results yielded two force values $F_1 = 11.42$ N and $F_4 = 4.35$ N, respectively. Additional information could be extracted by considering accumulative nature of the normal force. Radial variation of the relative accumulated forces $F_4(r)/F$ against the particle radius $r/R$ ($0 \leq r/R \leq 1$) is illustrated in Figure 7.
It is easy to detect from the graph that the obtained relationship between resultant forces $F_4/F_1 = 0.39$ indicates significant drop of the force with increase of the gap size. On the other hand, it could be state that the above ratio is much lower them the ratio of maximal pressures $p_{4,\text{max}}/p_{1,\text{max}} = 0.058$, which indicates different character of the pressure profiles.

### 4.3. Illustration of the space dependent properties

Several aspects are studied below. We try to separate the space defined effects influenced by the gap size and the time-dependent effects obtained by viscoelastic results.

A general tendency related to the gap size was already observed in earlier discussion indicating that the magnitude of the force and stiffness significantly varies with decrease of the initial distance between the aggregate spheres, i.e. the smaller the initial distance, the bigger the force needed to withdraw the sphere.

The influence of the initial gap was extracted by processing simulation results and demonstrated separately. Variations of the force values at the end of the loading at highest elongation period against the relative size $L_g/R$ of the gap are illustrated in Figure 8, while variations of the secant stiffness are given in Figure 9.

Here, viscoelastic behaviour is illustrated by dashed lines, while elastic results denoted by solid lines are presented for the sake of comparison. There, force and displacement are scaled with respect to interface properties and presented by dimensionless parameters $f = F/E_0L_gR$ and $u = U/L_g$, respectively.

Differences in deformation behaviour during interaction under tension may be considered by exhibition of the state variables. Illustrative sample is given in Figure 10, where contour plot of the maximal principal (tensile) logarithmic strain is plotted the central sections. Simulation results indicate extremely high values of strains in interface layer which coincide with those obtained by the other researches [10].

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**Fig. 7.** Variation of relative accumulated resultant force across the sphere radius. For various gaps

**Fig. 8.** Variation of the normal interaction force values against the size of the initial gap for various models

**Fig. 9.** Variation of the normal stiffness values against the size of the initial gap for various models

**Fig. 10.** Variation of maximum Principal Elastic strain: a) $L_g = 0.1$ mm; b) $L_g = 1.5$ mm
The pictures also show differences in the behaviour of the interface material. For the small gap, the tension is characterised by uniaxial stretching concentrated within the small cylinder. The increase of the gap size that that highest strains values occur in the middle of the gap between two particles.

4.4. Investigation of temporary behaviour

To evaluate temporary behaviour numerical results obtained by applying viscoelastic approach were additionally examined. Original simulation results are presented in terms of the normalised dimensionless force–displacement relationship. The curves illustrated in Figure 11 reflect typical character of viscous models.

In order to describe the viscoelastic behaviour, a general approach [27] considers the time-dependent force and the displacement relation \( F(U(t)) \) functions in a form of very complex function \( F(t) = G(U, t) \). It is used to name this function as relaxation function.

In the case linearity the relaxation function becomes only function of time \( G(t) \). In our case, geometrical nonlinearity was imposed. To illustrate influence of the nonlinearity, the secant stiffness is extracted from the curves in Figure 11 and, after scaling, is defined in the nondimensional forms. The obtained results are shown in Figure 12. Actually time variation of the stiffness may be interpreted as relaxation functions.

The results exhibit clear similarity of curves what means that influence of the gap has predicted by the geometry properties and the space resolution but this factor has minor influence to viscous properties. Dimensionless relaxation function for material defined by Prony series (4) is also presented for the sake of comparison. Results show slower relaxation of the interaction behavior when compared to the local relaxation of the material.

4.5. Discussion on the influence of the size of the gap

Summarizing results of the finite element simulation of the normal interaction of elastic particles in the confined viscoelastic solid under tension some important observations could be pointed out. Relaxation curves (Fig. 12) demonstrate that the size of interface gap has small contribution to temporary variation of stresses and strains. Consequently, similarity of non-dimensional relationships obtained after scaling should be valid independently on material model.

Investigation particle’s interaction via interface on the basis of purely continuum approach indicated existence of two different states separated by critical value of the gap size. Considerable stiffening of in constitutive behaviour of the matrix material is indicated below this size.

Our manifest suggests that this critical size is relevant to the Hertz contact radius obtained at the given load level \( F(t) \). Defining contact radius by classical expression [27].

We obtained \( a = 0.19R \). Referring variation of accumulated force given in Figure 7. We can find that major part of the resultant force is accumulated by the central part of the sphere within this radius.

Required force employed for interaction analysis could be chosen from the above results. Additionally, the circle with radius 0.2\( R \) yields 0.83\( F_1 \) and 0.59\( F_4 \). This means that radius of the representative volume and incompressible boundaries are applicable for simulation and has minor influence to the final results.

In the limit when gap size approaches zero \( L_g \rightarrow 0 \) we obtain the Hertz force \( F_H = 9.28 \) N [27].

\[
F_h = \frac{4}{3} E^* \cdot \sqrt{R \cdot u^2}
\]

were:
- \( F_h \) – Hertz contact force,
- \( E^* \) – contact elastic modulus;
- \( R \) – particle radius,
- \( u \) – indentation deep.

In the limit case the interaction may be interpreted as contact of two particles with parallel bond as it is used in bonded granular materials [27]. However, sophisticated microstructure models will be required to reflect influence of the finer particles in interface for real asphalt mixtures.

Regarding increase above the critical size of the gap, contributions of particles contact drops and infuse of material increases. The pressure will form decay zone between
particle and this zone will separated into two indicating motion of the single spheres. Qualitatively, pressure distributions evaluation of be alternatively define by fluid models [28].

5. CONCLUSIONS

Final conclusions are formulated as follows:

- Since interface material possesses observable changes of the geometry, influence of the geometric nonlinearity was evaluated by comparing linear and large deflection models. Observable up to 5–9% difference of normal force was found, therefore, nonlinear large deflection model is recommended for interaction analysis.

- Strain analysis shows that deformability of particles is negligibly small and could be neglected in the computational models. Consequently, particles could be presented by rigid surface, thereby, simplifying computational model and reducing the size of the model.

- Results clearly demonstrate influence of the viscosity of interface solid. For normal displacement of particles equal to 6.6% of particle radius R, yields reduction of the interaction force up to 56.7% when compared to purely elastic properties.

- Investigation of the size of initial inter-particle gap on the basis of purely continuum approach confirmed presence of interface layer around stiffer particle. Reduction of the inter-particle below critical size approximately equal to 0.066 of particle radius yields significant increase of interaction stiffness.

- It was shown that critical size is predicted by the geometry and is not sensitive to temporary behaviour. Future research is required to examine this effect regarding microstructure of interface.

References


